

DE LA SALLE UNIVERSITY – MANILA COLLEGE OF SCIENCE Mathematics Department

SYLLABUS

MTH643M/D
Modern Complex Analysis 1
3 units
(02) 536-0270, (02) 524-4611 loc. 420/413

COURSE DESCRIPTION

This is a course on complex numbers and complex plane, Cauchy-Riemann equations, Riemann surface and conformal mappings, infinite series, complex integration, singularities, integration, Cauchy integral theory, singularities, residue theory.

COURSE OBJECTIVES

The students will:

- 1. present complex numbers in various forms;
- 2. perform computations involving the elementary functions of a complex variable;
- 3. evaluate limits and determine the continuity or discontinuity of functions of a complex variable;
- 4. prove statements about functions of a complex variable that are consequences of the basic theorems in complex analysis;
- 5. apply the Cauchy Integral Theorems in the evaluation of certain integrals;
- 6. determine the region of convergence of a given power series;
- 7. state and apply the Residue Theorem in the evaluation of certain integrals.
- 8. Exhibit values that will allow the students to:
 - develop in the student interest and patience in reading and understanding, by himself/herself, printed materials in complex analysis.
 - develop the values of diligence, persistence and determination to succeed in solving the exercise problems presented in the course.
 - realize that the method of analytical thinking learned and developed while studying complex analysis my be adapted to real-life situations when the need to analyze realities to solve a concrete (nonmathematical) problem arises.

Topic/Subtopic	Learning Strategies/ Activities	Week/Meeting/ Hours
I. THE COMPLEX NUMBER FIELD	Lecture	6 Hours
	Group Discussion	

Topic/Subtopic	Learning Strategies/ Activities	Week/Meeting/ Hours
 1.1 Complex Numbers as Ordered Pairs 1.2 The Rectangular Form of a Complex Number 1.3 The Polar and Exponential Forms 1.4 Powers and Roots of Complex Numbers 1.5 The Extended Complex Plane, Stereographic Projection 	Problem Set	
II. FUNCTIONS OF A COMPLEX VARIABLE2.1 Functions as Mappings2.2 Limits of Functions2.3 Continuous Functions2.4 Differentiation of Functions2.5 Cauchy-Riemann Conditions for Analyticity2.6 Harmonic Functions	Lecture Group Discussion Problem Set	6 Hours
LONG TEST 1 III. THE ELEMENTARY FUNCTIONS AND THEIR PROPERTIES	Lecture Group Discussion Problem Set	1.5 Hours 6 Hours
3.1 The Exponential Function3.2 The Trigonometric Functions3.3 The Hyperbolic Functions3.4 Inverse Relations/Functions3.5 Multiple-valued Functions		
IV. INTEGRALS 4.1 Definite Integrals 4.2 Arcs and Contours 4.3 Contour Integrals	Lecture Group Discussion Problem Set	6 Hour
4.4 Antiderivatives & Independence of Paths		1 7 11
 V. SEQUENCES AND SERIES 5.1 Definitions and General Properties 5.2 Power Series, Region of Convergence 5.3 Functions as Power Series – Taylor's Series, Laurent's Series 5.4 Uniform Convergence 5.5 Algebraic Operation on Series 5.6 Differentiation and Integration of Power Series 	Lecture Group Discussion Problem Set	6 Hour
VI. THEORY OF RESIDUES 6.1 Definitions of Residue and Poles 6.2 The Residue Theorem 6.3 Residue at Poles 6.4 Improper Integrals	Lecture Group Discussion Problem Set	6 Hours
FINAL EXAMINATION		3 Hours

*OPTIONAL

TEACHING STRATEGIES/METHODOLOGY

Graduate Syllabus

To achieve the course objectives, a combination of lecture, group discussion and solutions of problem sets will be used.

COURSE REQUIREMENTS

•	Long Tests	50%
•	Final Examination	30%
•	Problem Sets	20%

SOURCES

- Ahlfors, Lars. Complex Analysis, McGraw-Hill Education, 1979.
- Brown, James. Complex Variables and Applications, McGraw-Hill Education (Asia), 2009.
- Churchill, Ruel Vance. Complex Variables and Applications, McGraw-Hill NewYork, 1984
- Gherardell, F. Complex Analysis, Springer Berling Heidelberg, 2011.
- Lang, Serge. Complex Analysis, Springer, New York, 1999.
- Pennisi, Louis. Elements of Complex Variables, Holt, Rinehart and Winston, 1976.

Noted by:

DR. ISAGANI B. JOS Chair, Mathematics Department

DR. JOSE SANTOS R. CARANDANG VI Dean, College of Science