

DE LA SALLE UNIVERSITY – MANILA COLLEGE OF SCIENCE Mathematics Department

SYLLABUS

| COURSE CODE | MSS513M |
|---|---|
| COURSE TITLE CLASS DAY & TIME ROOM NAME OF FACULTY | Introduction to the Theory of Statistical Inference |
| COURSE CREDIT | 3 Units |
| CONTACT NO. (DEPT) | (02) 536-0270, (02) 524-4611 loc. 420/413 |
| TERM/SCHOOL YEAR | |

COURSE DESCRIPTION

A course on the theory of estimation and hypothesis testing.

COURSE OBJECTIVES

The students will:

- 1. properly define basic concepts and state well known results in statistical inference;
- 2. demonstrate ability to evaluate estimators and construct appropriate interval estimates and tests of hypotheses;
- 3. show the capability of relating the theory of inference to real-world problems;
- cooperation through group study;
- honesty by claiming credit only for the work he has done;
- zeal and seriousness of intent to learn by participating actively in class discussion, doing his homework regularly and consulting his mentor;
- patience, perseverance and diligence by solving assigned exercises completely including the difficult ones;
- faith by doing what is right and giving his best in performing any assigned task;
- show concern for the community through sharing of know-how and resources during group discussion;
- self-reliance by being able to solve problems independently.

| Topic/Subtopic | Learning Strategies/ Activities | Week/Meeting |
|---|------------------------------------|--------------|
| 1. PROPERTIES OF A RANDOM SAMPLE | Lecture-Discussions | 7 hrs |
| 1.2 Sampling from the Normal Distribution | Problem Solving | |
| 1.3 Properties of the Sample Mean and Variance | Hands-on Exercises | |
| 1.4 The Derived Distributions: Student's t and Snedecor's F | | |
| 1.5 Order Statistics | | |
| 1.6 Convergence Concepts | | |
| 1.7 Convergence in Probability | | |
| 1.8 Almost Sure Convergence | | |
| 1.9 Convergence in Distribution | | |

| Topic/Subtopic | Learning Strategies/ | Week/Meeting |
|--|----------------------|--------------|
| | Activities | |
| 1.10Generating a Random Sample | | |
| QUIZ 1 | | 1 hr |
| 2. PRINCIPLE OF DATA REDUCTION | Lecture-Discussions | 12 hrs |
| 2.1 Introduction | Problem Solving | |
| 2.2 The Sufficiency Principle | Hands-on Exercises | |
| 2.3 Sufficient Statistics | | |
| 2.4 Minimal Sufficient Statistics | | |
| 2.5 Ancillary Statistics | | |
| 2.6 Sufficient, Ancillary, and Complete Statistics | | |
| 2.7 The Likelihood Principle | | |
| 2.8 The Likelihood Function | | |
| 2.9 The Formal Likelihood Principle | | |
| 2.10 The Equivariance Principle | | |
| QUIZ 2 | | 1 hr |
| 3. POINT ESTIMATION | Lecture-Discussions | 9 hrs |
| 3.1 Introduction | Problem Solving | |
| 3.2 Methods of Finding Estimators | Hands-on Exercises | |
| 3.3 Method of Moments | | |
| 3.4 Maximum Likelihood Estimators | | |
| 3.5 Bayes Estimators | | |
| 3.6 The EM Algorithm | | |
| 3.7 Methods of Evaluating Estimators | | |
| 3.8 Mean Squared Error | | |
| 3.9 Best Unbiased Estimators | | |
| 3.10 Sufficiency and Unbiasedness | | |
| 3.11 Loss Function Optimality | | |
| 4. HYPOTHESIS TESTING | Lecture-Discussions | 9 hrs |
| 4.1 Introduction | Problem Solving | |
| 4.2 Methods of Finding Tests | Hands-on Exercises | |
| 4.3 Likelihood Ratio Tests | | |
| 4.4 Bayesian Tests | | |
| 4.5 Union-Intersection and Intersection-Union Tests | | |
| 4.6 Methods of Evaluating Tests | | |
| 4.7 Error Probabilities and the Power Function | | |
| 4.8 Most Powerful Tests | | |
| 4.9 Sizes of Union-Intersection and Intersection-Union Tests | | |
| 4.10 p-Values | | |
| QUIZ 3 | | 1 hr |
| FINAL EXAMINATION | | 2 hrs |

COURSE REQUIREMENTS

- Quizzes and Long Exams
- Final Examination
- Problem Sets

SOURCES

- Casella, G. and Berger, R. (2002). *Statistical Inference*, 2/e. Duxbury, CA.
- Casella, G and Lehmann, E. (1998). *Theory of Point Estimation, 2/e.* Springer.
- Dekking, et. al. (2005). A Modern Introduction to Probability and Statistics. Springer.

- Roussas, G. (1997). A First Course in Mathematical Statistics, 2/e. Academic Press.
- Young, G.A. and Smith, R.L. (2005). *Essentials of Statistical Inference*. Cambridge University Press.

Noted by:

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