



# **COMANAL** – Complex Analysis

Prerequisite: ADVACA1

# Prerequisite to:

#### Instructor: \_\_\_\_\_ Consultation Hours: \_

#### Contact details: \_\_\_\_\_ Class Schedule and Room: \_\_\_\_

# **Course Description**

A course covering De Moivre's theorem, analytic functions of complex variables, harmonic functions, multiple-valued functions, contour integration, the Jordan Curve Theorem, the Cauchy Integral Theorem, Taylor Series, Laurent Series, residues and poles and conformal mappings.

# Learning Outcomes

On completion of this course, the student is expected to present the following learning outcomes in line with the Expected Lasallian Graduate Attributes (ELGA)

ELGA	Learning Outcome
Critical and Creative Thinker	At the end of the course, the student will apply
Effective Communicator	appropriate mathematical concepts, thinking
Reflective Lifelong Learner	processes, and tools in the solution to various
Service-driven Citizen	conceptual or real-world problems.

# **Final Course Output**

As evidence of attaining the above learning outcomes, the student is required to do and submit the following during the indicated dates of the term.

At the end of the course, the student will apply appropriate mathematical concepts, thinking processes, and tools in the solution to various conceptual or real-world problems	Learning Outcome	Required Output	Due Date
conceptual of real-world problems.	At the end of the course, the student will apply appropriate mathematical concepts, thinking processes, and tools in the solution to various conceptual or real-world problems.	Compilation of solved problems (problem sets) that will manifest the application of the concepts learned	Week 13

# Rubric for assessment

CRITERIA	Excellent (4)	Good (3)	Satisfactory (2)	Needs Improvement (1)
Understanding of mathematical concepts (25%)	Shows complete understanding of the underlying mathematical concepts and principles needed to solve the problem.	Shows nearly complete understanding of the problem's mathematical concepts and principles.	Shows some understanding of the mathematical concepts and principles needed to solve the problem.	Shows very limited understanding of the problem's mathematical concepts and principles.
Clarity of Explanation (25%)	Explanation is well- written, complete and unambiguous. Terminologies and symbols are used correctly.	Explanation is clear but few simple details are missed. Terminologies and symbols are used appropriately.	Explanation is little difficult to understand. Some symbols and notations are used inappropriately.	Explanation is difficult to understand.
Accuracy of Computations (25%)	Computations are correct and the final answer is arrived at.	Computations are correct except for some minor errors.	Computations have some major errors.	Incorrect computations.
Understanding of methods of proof (25%)	Shows correct understanding of the method of proof. Statements are logical and the desired conclusion is arrived at.	Shows correct understanding of the method of proof. The proof proceeded logically except for a few minor errors.	Shows correct understanding of the method of proof but there are major errors in reasoning.	Lacks understanding of the method of proof but an attempt to solve the problem is evident.

Grading System						
	FOR EXEMPTED	FOR STUDE FINAL I	ENTS with EXAM	<b>Scale:</b> 95-100%	4.0	
	STUDENTS (w/out Final Exam)	with no missed quizzes	with one missed auiz	89-94% 83-88% 78-82% 72-77%	3.5 3.0 2.5 2.0	
Average of quizzes	95%	60%	50%	66-71% 60-65%	1.5 1.0	
Other requirements	5%	10%	10%	<60%	0.0	
Final exam	-	30 %	40%			

# Learning Plan

LEARNING OUTCOME	ΤΟΡΙϹ	WEEK NO.	LEARNING ACTIVITIES
At the end of the course, the student will apply appropriate mathematical concepts, thinking processes, and tools in the solution to various conceptual or real- world problems.	<ul> <li>I. THE COMPLEX NUMBER FIELD         <ol> <li>1.1. Complex Numbers as Ordered Pairs</li> <li>1.2. The Rectangular Form of a Complex Number</li> <li>1.3. The Polar and Exponential Forms</li> <li>1.4. Powers and Roots of Complex Numbers</li> <li>1.5. The Extended Complex Plane, Stereographic Projection</li> </ol> </li> </ul>	Week 1-2 (6 HRS)	<ul> <li>Library work</li> <li>Cooperative Learning</li> <li>Skills exercises</li> <li>Student self- assessment and reflection</li> <li>Quizzes</li> <li>Seatworks</li> </ul>
	QUIZ 1	1 HR	
	II. FUNCTIONS OF A COMPLEX VARIABLE 1.1. Functions as Mappings 1.2. Limits of Functions 1.3. Continuous Functions 1.4. Differentiation of Functions 1.5. Cauchy-Riemann Conditions for Analyticity 1.6. Harmonic Functions	Week 3-5 (7 HRS)	
	<ul> <li>III. THE ELEMENTARY FUNCTIONS AND THEIR PROPERTIES         <ol> <li>The Exponential Function</li> <li>The Trigonometric Functions</li> <li>The Hyperbolic Functions</li> <li>Inverse Relations/ Functions</li> </ol> </li> <li>The Complex Logarithmic Function</li> </ul>	Week 5-7 (5 HRS)	
	QUIZ 2 V. INTEGRALS 1.1. Definition and General Properties of the Integral 1.2. Contour Integrals 1.3. The Cauchy-Goursat Integral Theorem	1 HR Week 8-9 (7 HRS)	

	<ul><li>1.4. The Cauchy Integral Formula</li><li>1.5. Morera's Theorem</li></ul>		
v.	<ul> <li>SEQUENCES AND SERIES</li> <li>1.1. Definition and General Properties</li> <li>1.2. Power Series, Region of Convergence</li> <li>1.3. Functions as Power Series – Taylor's Series, Laurent's Series</li> </ul>	Week 10-12 (8 HRS	
VI.	<ul> <li>THEORY OF RESIDUES</li> <li>1.1. Definition of Residues and Poles</li> <li>1.2. The Residue Theorem</li> </ul>	Week 13 (3 HRS)	
	QUIZ 4	1 HR	
	1.3. Residues at Poles 1.4. Improper Integrals		
	Final Examination	2 HRS	

#### References

Pennisi L.L. (1976) Elements of Complex Variables (2<sup>nd</sup> Edition). Manila: National Bookstore

Ahlfors L.V. (1979) Complex Analysis (3rd Edition). NY: McGraw-Hill

Conway J.H. and Howell R.W. (2006) Complex Analysis for Mathematics and Engineering (5<sup>th</sup> Edition) Andreescu, T.(2005) Complex Numbers from A to Z, Birkhauser

Cohen, H. (2008) Complex Analysis with Applications in Science & Engineering (2<sup>nd</sup> Edition). Springer Eiderman, V.Y. and Samokhin, M.V.(2005). Selected Topics in Complex Analysis, Birkhauser Gilman, J.P.(2008) Complex Analysis, Springer

# **Online Resources**

http://www.umn.edu/~arnold/502.597/complex.pdf. http://www.math.ucla.ed/%7ETao/resource/general/132.100w/ http://www.math.lsu.ed/`neubrand/notes.pdf

# **Class Policies**

- 1. The required minimum number of quizzes for a 3-unit course is 3, and 4 for 4-unit course. No part of the final exam may be considered as one quiz.
- 2. Cancellation of the lowest quiz is not allowed even if the number of quizzes exceeds the required minimum number of quizzes.
- 3. As a general policy, no special or make-up tests for missed exams other than the final examination will be given. However, a faculty member may give special exams for
  - A. approved absences (where the student concerned officially represented the University at some function or activity).
  - B. absences due to serious illness which require hospitalization, death in the family and other reasons which the faculty member deems meritorious.
- 4. If a student missed two (2) examinations, then he/she will be required to take a make up for the second missed examination.
- 5. If the student has no valid reason for missing an exam (for example, the student was not prepared to take the exam) then the student receives 0% for the missed quiz.
- 6. Students who get at least 89% in every quiz are exempted from taking the final examination. Their final grade will be based on the average of their quizzes and other prefinal course requirements. The final grade of exempted students who opt to take the final examination will be based on the prescribed computation of final grades inclusive of a final examination. Students who missed and/or took any special/make-up quiz will not be eligible for exemption.
- 7. Learning outputs are required and not optional to pass the course.
- 8. Mobile phones and other forms of communication devices should be on silent mode or turned off during class.

- 9. Students are expected to be attentive and exhibit the behavior of a mature and responsible individual during class. They are also expected to come to class on time and prepared.
- 10. Sleeping, bringing in food and drinks, and wearing a cap and sunglasses in class are not allowed.
- 11. Students who wish to go to the washroom must politely ask permission and, if given such, they should be back in class within 5 minutes. Only one student at a time may be allowed to leave the classroom for this purpose.
- 12. Students who are absent from the class for more than 5 meetings will get a final grade of 0.0 in the course.
- 13. Only students who are officially enrolled in the course are allowed to attend the class meetings.

Approved by:

# DR. ARTURO Y. PACIFICADOR, JR.

Chair, Department of Mathematics

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